Abstract— In this paper, a double layer stopband Frequency Selective Surface (FSS) for Ultra-Wide Band (UWB) applications is presented. The proposed FSS consists of two cascaded conventional FSS, one with double square loops and other with square loops. The –10dB frequency band from 3.00 GHz to 11.64 GHz is achieved, with a fractional bandwidth of 149%. Effects of angular stability and polarization independence over the frequency response are investigated and conclusions are presented. In order to show transmission performance, the FSS was simulated by ANSYS HFSS. The FSS shows angular stability and polarization independence in entire UWB band (3.10 – 10.60 GHz). A prototype was built and measurements were performed. A good agreement between simulated and measured results was observed.

Index Terms— FSS, UWB response, Angular stability, Polarization independence.

I. INTRODUCTION

Frequency Selective Surfaces (FSS) are bi-dimensional periodic arrays of metallic patches on dielectric layer. FSS acts as a spatial filter which reflect some frequencies and transmit other frequencies. This response is dependent on polarization and angle of incidence of electromagnetic waves, geometry of patch, periodicity of unit cells, thickness and permittivity of the substrate [1].

FSS has been widely used in different applications as radome [2], spatial filter [3], and polarizer [4] due to possibility of controlling transmission and reflection characteristics of electromagnetic incident waves [5]. Recently, we can observe huge progress of multifunctional systems which usually contains several antennas with different operating frequencies [6], [7]. So, an ultra-wideband (UWB) FSS could be used to improve UWB antennas’ performance, for those systems. In many cases, the angular range reached 30 degree or even more [8], therefore, it is essential that an UWB FSS provides steady frequency response in wide incident angles and also polarization independence.

Many researchers have proposed UWB FSS. A multi-layer FSS was proposed in [9] to provide an UWB bandwidth with angular stability, but the FSS operates from 5.85 – 18.45 GHz. In [10], the authors proposed an UWB FSS using compact elements to obtain a good transmission property when the
incident angle was from 0 to 45 degree, the covered band was from 4 to 14 GHz. The authors proposed in [11] an UWB band pass FSS with reduced sensitivity to incident angles and bandwidth attains 8.64 GHz (3.49 – 12.13 GHz), providing stable performance at incident angles for both vertical and horizontal polarizations. In [12], the authors proposed a double layer FSS for wideband applications. The proposed FSS reached a fractional bandwidth of 56 % from 4 to 7 GHz and with angular stability from 0 to 60 degree.

All those proposed FSS did not cover entire band of UWB applications (3.10 – 10.60 GHz). So, in this paper we propose a cascaded structure that uses two FSS with well-known geometries in literature, the double square loop and the square loop, to obtain an UWB FSS with angular stability and polarization independence covering the entire UWB band. To optimize the design of FSS, neural networks were used.

II. UWB STRUCTURE DESCRIPTION

The idea of cascading several FSS is not new and it was presented in [13]. The idea is to cascade two or more FSS to obtain a wide band response, but the structure presented in [13] has two problems, it was not designed to operate in UWB band (3.10 – 10.60 GHz) and it does not present polarization independence and angular stability.

So, in this work, the aim is to design a cascaded structure with two FSS to apply in the UWB technology (3.10 GHz – 10.60 GHz). To reach this objective, we used two geometries, the square loop and the double square loop. We chose these two geometries because they provide polarization independence and angular stability.

The proposed structure is illustrated in Fig. 1. It is a two FSS cascaded using two different geometries as unit cells printed on a dielectric substrate. The dielectric substrate used is FR4 with dielectric constant, \( \varepsilon_r = 4.4 \) and dielectric loss tangent of 0.02.

![Fig. 1. Representation of cascaded FSS with double square loop (FSS 1) and square loop (FSS 2).](image)

Fig. 2 illustrates the cells’ geometries. Fig. 2(a) illustrates the double square loop geometry used in FSS1 and its parameters. Fig. 2(b) illustrates the square loop geometry used in FSS2 and its parameters.

In Fig. 2(a), \( p \) is the periodicity, \( d_1 \) and \( w_1 \) are length and strip width of the outer square loop; \( d_2 \) and \( w_2 \) are length and strip width of the inner square loop. \( g_2 \) and \( g_1 \) are, respectively, the gap between outer
and inner square loops and between two outer square loops. In Fig. 2(b), \( p \) is the periodicity, \( d \) and \( w \) are length and strip width of the square loop, \( g \) is the gap between two square loops.

![Cascaded FSS cells' geometries: (a) Double square loop, (b) Square loop.](image)

Fig. 2. Cascaded FSS cells' geometries: (a) Double square loop, (b) Square loop.

III. UWB STRUCTURE MODELLING

These proposed UWB FSS must have desirable features as polarization independence and angular stability for oblique incidence of plane waves. Fig. 3 gives an overview of the electromagnetic optimization technique and neural network training process used. The training process starts with a full-wave parametric analysis, we obtain accurate database that maps the FSS frequency responses (resonance frequency and bandwidth) input and output physical dimensions.

For the FSS optimization, a developed radial base function (RBF) neural network (NN) is used for fast and accurate computation of the cost function if its architecture and training algorithm are properly chosen. The RBF-NN replaces repetitive full-wave numerical simulations and overcomes the associated high computational cost. In final step, FSS prototypes are fabricated with optimal design parameters and measured for verification of the technique accuracy.

From the generation of database, one RBF-NN was used as a tool to optimize the FSS double square loop and another to square loop parameters. The network architectures can be seen in Fig. 4.

The values of \( \tilde{x}_1, \tilde{x}_2, \tilde{x}_3, ..., \tilde{x}_n \) represent the input layer in which normalized values are provided to the NN. In this work, the data at the input layer are the normalized values of the resonance and bandwidth frequencies (\( \tilde{x} \)), that is, \( \tilde{x} = x/x_{\text{max}}, x_{\text{max}} \) are the maximum values of each input parameter within the data bank. In the output layer, the NN will display the values of geometry dimensions and dielectric thickness normalized \( \tilde{y} \). Then, the final value is \( y = \tilde{y}.y_{\text{max}} \).
In order, to be able to learn the NN two steps are required: training and validation. The training of the NN consists of adjusting the values of the weights $W^{(1)}$ and $W^{(2)}$, which are the synaptic weights of the connections between the entry and the intermediate layer and, from the intermediate layer to the output layer, respectively. With the adjustment of the weights, the NN extracts the characteristics of the database and has generalization capacity. In the middle layer of proposed NN, whose learning occurs unattended, the activation function is a Gaussian type. Gaussian function is commonly used as the radial basis in RBF neural network.

The method of adjusting the weights $W^{(1)}$, a unsupervised learning, was used $k$-means [14]. $K$-means algorithm is a kind of cluster algorithm, it was proposed by J. B. MacQueen [15]. The main aim of $k$-means is to position $k$-Gaussian centers in regions where input patterns will tend to cluster. The centers are represented by the synaptic weights ($W^{(1)}$) of the NN and the variance of each Gaussian activation functions was calculated by the criterion of the mean square distance.
Fig. 4. RBF-NN used in optimization technique: (a) Double Square Loop; (b) Square Loop.

The k-means algorithm used to adjust $W^{(1)}$, was developed as follows, in the initial step of the algorithm, the first values of the database samples were used as initial $W^{(1)}$, from that value was calculated the Euclidean distance between the samples and $W^{(1)}$, considering each neuron at one time. After the calculation with all samples, the neuron with the shortest distance is selected, aiming to group the sample to the nearest center. The selected sample is assigned to a group $A$. To adjust all weights $W^{(1)}$ from group $A$, as (1):

$$W^{(1)} = \frac{1}{m} \sum_{x \in A} x$$

$x$ are the samples and $m$ is the number of samples belonging to group $A$. 
This instruction is repeated until there are no more changes in group A between the interactions. After this, the variance of each of the Gaussian activation functions is calculated by the criterion of the mean square distance, according to (2).

\[ \sigma^2 = \frac{1}{m} \sum_{x \in A} \sum (x - W^{(1)})^2 \]  

In the output layer, the weights \( W^{(2)} \) are adjusted after the intermediate layer, and for its adjustment was used the learning algorithm that implements the generalized delta rule, whose objective, in a supervised way, is to minimize the error mean square given in (3):

\[ MSE = \frac{1}{q} \sum_{i=1}^{q} E(i) \]  

where \( E(i) \) is the quadratic error consisting of the difference between the desired value and the response of the output layer for each sample \( i \), and \( q \) is the number of samples at one time. \( E(i) \) is:

\[ E(i) = \frac{1}{2} \sum_{n=1}^{n_2} \left( d_n(i) - y_n(i) \right)^2 \]  

where \( d_n(i) \) is the nth desired response and \( y_n(i) \) is the nth NN output.

The activation function used in neurons of the output layer was the sigmoid function. This function was the first to be tested in the network, because it is computationally easy to perform, as it obtained good results, no other was tested.

As a criterion of stopping, the mean square error (MSE) to be reached was used. When the MSE reached and the MSE of validation differentiated by 20%, it was considered that the neural network converged and the process ended, or if the neural network doesn’t converge after 200,000 epochs.

To train and validate the neural networks to optimize the parameters of square loop FSS and double square loop FSS, a database was generated with the parameters described in Table 1 and Table 2. To extract the values of resonance frequency and bandwidth it was utilized ANSYS HFSS software. And all simulations were performed a range of frequency of 1 to 40 GHz. And the substrate utilized was FR4.

### Table 1. Values of parameters to generate the database of square loop FSS.

| Square Loop FSS |  
|-----------------|---|
| **Periodicity (p)** | 5; 10; 15; 20 |
| **Length (d)** | 3.5; 6; 7.5; 10; 13; 18 |
| **Width (w)** | 0.1; 0.15; 0.2; 0.25; 0.3; 0.35; 0.4; 0.45; 0.5; 0.6; 0.8; 1; 1.5; 2; 2.5; 3; 3.5; 4; 4.5; 5 |
| **Thickness (h)** | 0.8; 1.2; 1.6 |
Not all combinations of Table 1 are possible, and the database was composed only of the samples that presented one resonance frequency. The database was formed by 104 samples.

To optimize square loop FSS, the resonance frequency and bandwidth values are presented in the input layer \((x)\) whose maximum values \((x_{\text{max}})\) were 21 GHz and 10.5 GHz, respectively. At the output \((y)\), the values of \(d, p, w\) and \(h\), whose maximum values \((y_{\text{max}})\) were: 18 mm, 20 mm, 5 mm and 1.6 mm, respectively.

For the training of NN from the database generated by the FSS with square loop geometry, were inserted: 2 neurons in the input layer that correspond to the resonance frequency and bandwidth; 36 neurons in the hidden layer and 4 neurons in the output layer that correspond to the constructive parameters of the square loop geometry. The number of neurons in the middle layer in each NN was adjusted from the minimum number of epochs to arrive at the required mean square error in training.

In the NN training, it was noticed that the learning rate of 0.006 and the mean square error to be reached equal to 0.05 in training stage were sufficient for the network to perform the FSS optimization at the desired frequency and bandwidth in the project. 80% of the data were used for training and the rest was used for validation. The test of NN was realized with project parameters, as seen in Table 3. Fig. 5 shows the training and validation results for the RBF-NN. The NN reach the aim around 50,000 epochs.

![Graph showing training and validation results for RBF-NN](image)

In the generation of the database for training and validation of neural network, the FSS parameters \(d_1, d_2, p, w_1, w_2\) and \(h\) were varied according to Table 2.

Not all combinations of Table 2 are possible, and the database was composed only of the samples that presented double band response. The database was formed by 287 samples.
Table 2. Values of parameters to generate the database of double square loop FSS.

<table>
<thead>
<tr>
<th>Parameters</th>
<th>Values (mm)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Periodicity (p)</td>
<td>5; 10; 12; 15; 16; 20.</td>
</tr>
<tr>
<td>Length (d₁)</td>
<td>4.5; 7; 7.5; 8; 9; 9.6; 10.2; 11.5;</td>
</tr>
<tr>
<td></td>
<td>12; 13; 15; 1.</td>
</tr>
<tr>
<td>Width (w₁)</td>
<td>0.1; 0.15; 0.2; 0.25; 0.3; 0.35; 0.4; 0.5; 0.6; 1;</td>
</tr>
<tr>
<td></td>
<td>1.5; 2; 2.5; 3.</td>
</tr>
<tr>
<td>Length (d₂)</td>
<td>2.5; 5; 6.5; 7; 7.2; 8; 9; 12; 15;</td>
</tr>
<tr>
<td>Width (w₂)</td>
<td>0.1; 0.15; 0.2; 0.25; 0.3; 0.35; 0.4; 0.5; 0.6; 1;</td>
</tr>
<tr>
<td></td>
<td>1.5; 2; 2.5; 3; 3.5; 4</td>
</tr>
<tr>
<td>Thickness (h)</td>
<td>0.8; 1.2; 1.6.</td>
</tr>
</tbody>
</table>

For the optimization of the double square loop, the values of the resonance frequency of the first band \(f_{r1}\) and its bandwidth \(BW_1\), the resonance frequency of the second band \(f_{r2}\) and its bandwidth \(BW_2\) are presented to the network input \(x\), whose maximum values \(x_{\text{max}}\) were: 18 GHz, 5.5 GHz, 45 GHz and 8 GHz, respectively. At the output \(y\), the values of \(d_1, d_2, p, w_1, w_2\) and \(h\), whose maximum values \(y_{\text{max}}\) are: 19 mm, 15 mm, 20 mm, 3 mm, 4 mm and 1.6 mm.

The RBF-NN training with the use of the FSS database generated by the double square loop geometry was performed with the following parameters: 4 neurons were inserted in the input layer corresponding to the resonance frequencies and bandwidths, 40 neurons in the hidden layer and 6 neurons in the output layer that correspond to the constructive parameters of the square loop geometry \((h, p, d_1, d_2, w_1, w_2)\).
Learning rate was 0.1, the mean square error to be reached was 0.05 in training stage and the evolution of the network in its training and validation can be visualized in Fig. 6. 80% of the data were used for training and the rest was used for validation. The test of NN was realized with project parameters, as seen in Table 4. The NN reach the aim around 14,000 epochs.

In the NN trained with the square loop database, was entered the input parameters: resonance frequency and bandwidth and, as output parameters, we found the values for the optimized FSS, as visualized in Table 3.

### Table 3. Square loop optimized.

<table>
<thead>
<tr>
<th>Square Loop Design (FSS 2)</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Input Parameters</strong></td>
</tr>
<tr>
<td>( fr ) &amp; ( BW )</td>
</tr>
<tr>
<td>5.8 GHz &amp; 3.0 GHz</td>
</tr>
<tr>
<td><strong>Output Parameters</strong></td>
</tr>
<tr>
<td>( h ) &amp; ( p ) &amp; ( D ) &amp; ( W )</td>
</tr>
<tr>
<td>1.2 mm &amp; 12.6749 mm &amp; 11.0918 mm &amp; 1.2874 mm</td>
</tr>
</tbody>
</table>

The same procedure was performed for the NN trained with the double square loop database. The input parameters: resonance frequency and bandwidth and the output parameters were the optimized values of the FSS, according to Table 4.

### Table 4. Double square loop optimized.

<table>
<thead>
<tr>
<th>Double Square Loop Design (FSS 1)</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Input Parameters</strong></td>
</tr>
<tr>
<td>( fr_1 ) &amp; ( BW_1 ) &amp; ( fr_2 ) &amp; ( BW_2 )</td>
</tr>
<tr>
<td>3.0 GHz &amp; 1.5 GHz &amp; 9.0 GHz &amp; 3.0 GHz</td>
</tr>
<tr>
<td><strong>Output Parameters</strong></td>
</tr>
<tr>
<td>( h ) &amp; ( P ) &amp; ( d_1 ) &amp; ( d_2 ) &amp; ( w_1 ) &amp; ( w_2 )</td>
</tr>
<tr>
<td>1.2 mm &amp; 12.6749 mm &amp; 12.1712 mm &amp; 8.4438 mm &amp; 0.4268 mm &amp; 1.1075 mm</td>
</tr>
</tbody>
</table>

### IV. NUMERICAL AND EXPERIMENTAL RESULTS

After modeling with the RBF-NN the physical dimensions necessary to obtain the desired frequency responses for the two proposed structures, FSS1 and FSS2, simulations of the transmission characteristics of these structures were done in the ANSYS HFSS software. Fig. 7 illustrates these simulations. The gray areas are the desired bandwidths. For FSS1, simulations obtain \( BW = 2.84 \text{ GHz} \) and \( fr = 6.0 \text{ GHz} \), very close to desired values (Table 3). For FSS2, simulations obtain \( BW_1 = 1.23 \text{ GHz} \), \( fr_1 = 3.2 \text{ GHz} \) and \( BW_2 = 2.74 \text{ GHz} \) and \( fr_2 = 9.1 \text{ GHz} \), also very close to desired values (Table 4). So, bandwidth and resonant frequency requirements met. Differences did not reach 10%. 
After the design of the isolated FSS, we performed a parametric study to find the best distance (air gap) between cascaded FSS (Fig. 1). In this study, we varied the gap value from 0 to 30 mm. After this parametric analysis, we realized that an ultra-wide bandwidth would be possible with the gap value of 5 mm. Thus, we cascaded the two FSS and simulated the structure in the ANSYS HFSS software. The results can be seen on Fig. 8. Considering $|S_{11}| = -10$ dB, bandwidth obtained was 7.6 GHz (3.05–10.65 GHz), sufficient for UWB, that is 7.5 GHz (3.10–10.60 GHz). So, simulations show that our proposed cascaded FSS can be used in UWB applications.

It is also important that the cascaded structure has polarization independence and angular stability. So, we simulated the transmission characteristic for vertical and horizontal polarization and for different angles of incidence. In Fig. 9, we can see the frequency response of the FSS designed for vertical polarization. The incident angles are changed from 0 to 30 degrees; this is because our setup measurement has no capability to measure bigger angles. It may be noted that, for our frequency range
of interest, there is no degradation in bandwidth. This shows that the geometry is stable in terms of incidence angles, for vertical polarization.

In Fig. 10 we can see the frequency response of the FSS designed for different angles of incidence and horizontal polarization. It may be noted that, although some degradation has occurred near 9 GHz, this degradation does not exceed – 10 dB, for the $|S_{11}|$, maintaining the performance of the structure, as in the case of vertical polarization. This shows that the structure has polarization independence and angular stability.

To validate the analysis performed, prototypes were built and experimental characterizations were performed. Thus, we could compare the simulated results with measurements. The measurements were carried out using a vector network analyzer (VNA) from Agilent, model E5071C, two horn antennas of the manufacturer A. H. Systems, model SAS-571 (700 MHz to 18 GHz), positioned in direct line of sight. A photograph of measurement setup and of device under test (DUT) is shown in Fig. 11. The absorber is used to avoid diffraction around the edges of the panel.
dimensions provided by the RBF-NN must be truncated. So, for FSS1 the dimensions used in fabrication were: $h = 1.2 \text{ mm}; p = 12.7 \text{ mm}; d_1 = 12.2 \text{ mm}; d_2 = 8.4 \text{ mm}; w_1 = 0.4 \text{ mm};$ and $w_2 = 1.1 \text{ mm}$. For FSS2 the dimensions used in fabrication were: $h = 1.2 \text{ mm}; p = 12.7 \text{ mm}; d = 11.1 \text{ mm}$ and $w = 1.3 \text{ mm}$.

Fig. 11. Measurement setup.

Fig. 12 illustrates the cascade FSS, with plastic spacers and screws.

Fig. 12. Cascade FSS.

In Fig. 13 we can see a comparison between numerical and measured results for FSS1 for normal incidence. Desired results were: $f_1 = 3.0 \text{ GHz}$ and $BW_1 = 1.5 \text{ GHz}; f_2 = 9.0 \text{ GHz}$ and $BW_2 = 3.0 \text{ GHz}$. Simulated results were: $f_1 = 3.25 \text{ GHz}$ and $BW_1 = 1.18 \text{ GHz}; f_2 = 9.13 \text{ GHz}$ and $BW_2 = 2.51 \text{ GHz}$. Measured results were: $f_1 = 3.46 \text{ GHz}$ and $BW_1 = 1.49 \text{ GHz}; f_2 = 9.68 \text{ GHz}$ and $BW_2 = 3.66 \text{ GHz}$. The measured and simulated results show good agreement. The main difference is due to the truncation on physical dimensions because the limitation of manufacture.
In Fig. 1 we can see a comparison between numerical and measured results for cascaded FSS for normal incidence. Desired results were: $f_r = 5.5$ GHz and $BW = 3.0$ GHz. Simulated results were: $f_r = 6.0$ GHz and $BW = 2.8$ GHz. Measured results were: $f_r = 6.0$ GHz and $BW = 3.8$ GHz. The measured and simulated results show good agreement.

After built the isolated FSS, we cascaded the two FSS with an air gap of 5 mm. Fig. 1 compares simulated and measured results. The bandwidth obtained for simulated results was 7.60 GHz (3.05 – 10.65 GHz) and for measurements was 8.64 GHz (3.00 – 11.64 GHz).

In figures 16 and 17 we can see measured results of vertical and horizontal polarization, respectively, with oblique incidence. Measured results show that the bandwidth does not suffer degradation in both cases, for different incidence angles, confirming the angular stability and polarization independence. Angles of incidence were changed from 0 to 30 degrees because we have limitations with measurement setup.
Fig. 15. Comparison between simulated and measured results for cascaded structure.

Fig. 16. Measured results for oblique incidence and vertical polarization.

Fig. 17. Measured results for oblique incidence and horizontal polarization.
V. CONCLUSIONS

In this article we proposed a structure formed by two cascaded FSS to obtain UWB frequency response. The geometries chosen for the FSS design were the double square loop and the square loop, since both have good angular stability and polarization independence. Computational intelligence tools were used to optimize the FSS design, reducing the time and computational effort of the project. The cascade technique was chosen because it proved efficient in other studies [13]. The final structure obtained a stop-band response across the UWB frequency range (3.1 – 10.6 GHz), and can be used in different applications, such as microstrip antenna optimization. To validate the analysis performed prototypes were fabricated and measurements were performed. A good agreement between numerical and experimental results was observed. The experimental results proved the UWB response, the polarization independence and the angular stability of the structure.

ACKNOWLEDGMENT

The authors express their sincere thanks to National Council of Research and Development – CNPq for supporting the research work over the project 303693/2014-2.

REFERENCES

[14] Zhenxiang Xing, Hao Guo, Shuhua Dong, Qiang Fu, Jing Li, “RBF Neural Network Based on K-means Algorithm with Density Parameter and Its Application to the Rainfall Forecasting”, 8th International Conference on Computer and Computing Technologies in Agriculture (CCTA), Sep 2014, Beijing, China.